

A tale of two non-SUSY DGKT vacua

Joan Quirant



Based on: [2110.11370](#) with F. Marchesano and D. Prieto, [2204.00014](#) and [22XX.XX](#)
with F. Marchesano and M. Zatti

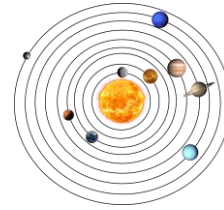
String phenomenology 2022

Motivation

- Current **observations** teach us that in our universe there appears to be

- **Scale separation**

- **No SUSY** (at energies tested so far)

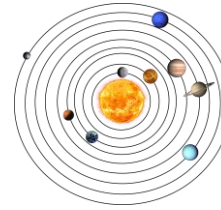


Motivation

- Current **observations** teach us that in our universe there appears to be

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- Current **computations** teach us that in string theory

- It is **difficult** to obtain fully controlled models with **scale separation**



- **Non-SUSY vacua** seem to be always **unstable**

In this talk we will focus on these problems



Motivation

- Work with **non-SUSY** vacua of **DGKT** type



or



- Nice **properties**: 😊
 - Parametrically **scale separated** (at large volume, weak coupling)
 - **Perturbative stable**
- Not that nice properties: 😞
 - Complete solution to the 10d equations not known (**smearing approximation**)
 - **Non-perturbative stability?**

Contents

- 1) Introduction and context
- 2) Conformal dual?
- 3) AdS instability conjecture (II)
- 4) Conclusions


DGKT: a quick start guide

DeWolfe, Giryavets, Kachru, Taylor '05; Cámara, Font, Ibáñez '05

- **DGKT** vacua: massive type IIA compactified on a CY orientifold with
 - NSNS H_3 and RR internal fluxes G_0, G_2, G_4, G_6 (democratic formulation $\mathbf{G} = \text{vol}_4 \wedge \tilde{G} + G, \tilde{G} \sim *_6 G$).

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- They are very trendy these days 
 - Obtained **using** directly the **4d effective theory** and not solving the 10d EOM
 - Intersecting orientifold O6-planes: **no complete uplift** is known (only if the sources are smeared* Acharya, Benini, Valandro '07). Approximate uplift beyond the smearing approximation in Junghans '20, Marchesano, Palti, JQ, Tomassielo '20
 - Phenomenologically interesting : **scale separation** $R_{KK} \sim R_{AdS}^{7/9}$ at large volume and small string coupling.
 - In **tension** with the **strong AdS distance conjecture** (only for the SUSY vacua) Lust, Palti, Vafa '19



* $dF = H + \delta \rightarrow$ Smearing approximation: $\delta = -H$

DGKT: a quick start guide

- Several **branches** of vacua (beyond the original SUSY one) derived in Marchesano, JQ, '19. Focus on:
 - **Non-SUSY** _{G_4} related to the standard SUSY DGKT vacuum by $G_4 = -G_4^{\text{SUSY}}$
 - **Non-SUSY** _{G_2} which has a harmonic component for G_2 different from 0, $G_2^{\text{harmonic}} \neq 0$
 - Perturbatively stable (checked in Marchesano, JQ '19) ✓
 - Non-perturbative stability for the **Non-SUSY** _{G_4} **studied** in Aharony, Antebi, Berkooz '08; Narayan, Trivedi '10 using D4, D6 and D2 DW. At most **marginal** decays

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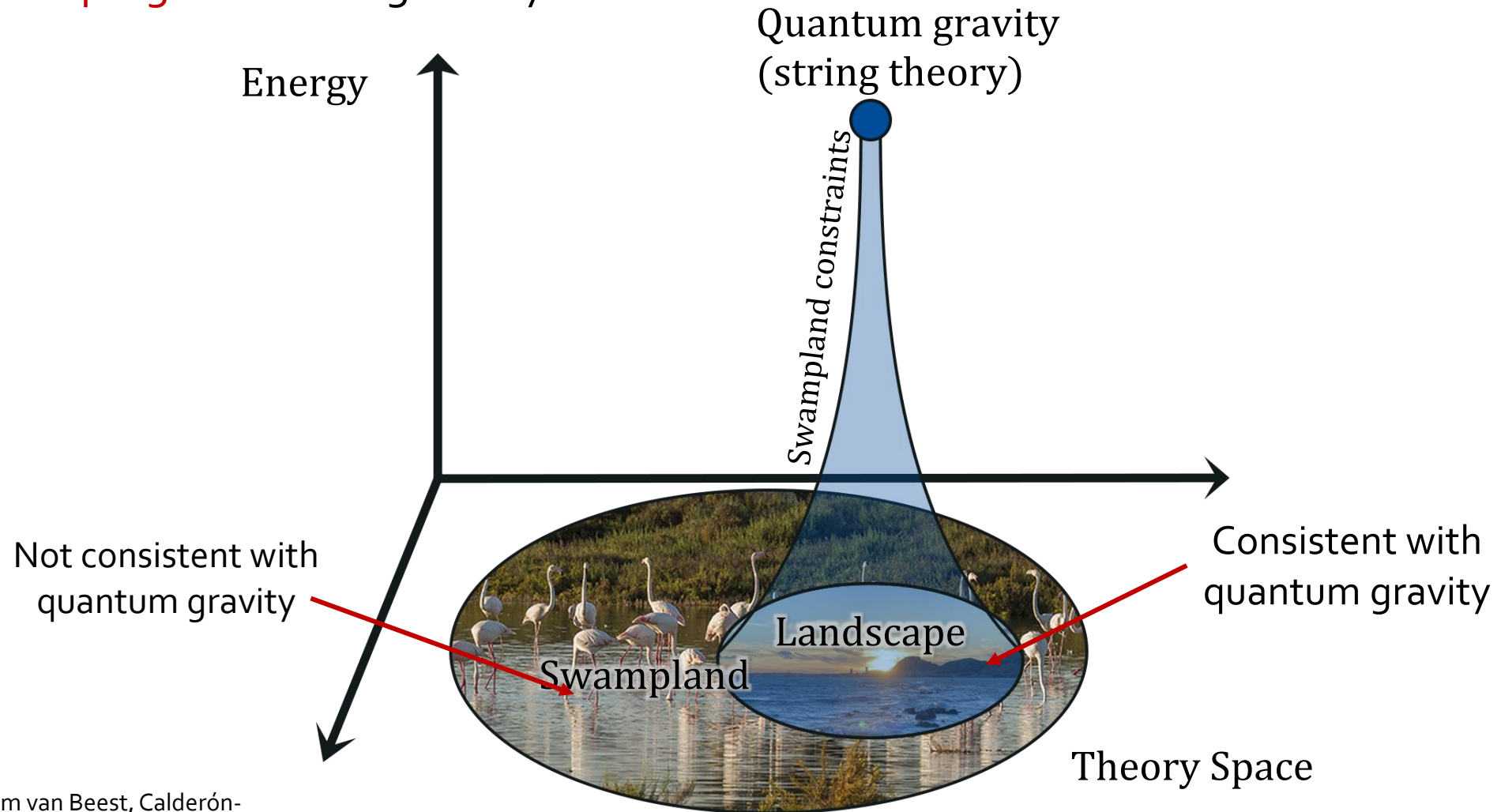


- What we can say about the validity/stability of the **Non-SUSY** _{G_4} and the **Non-SUSY** _{G_2} branches?

Two main tools: AdS/CFT correspondence and DW branes

A swampland in the room

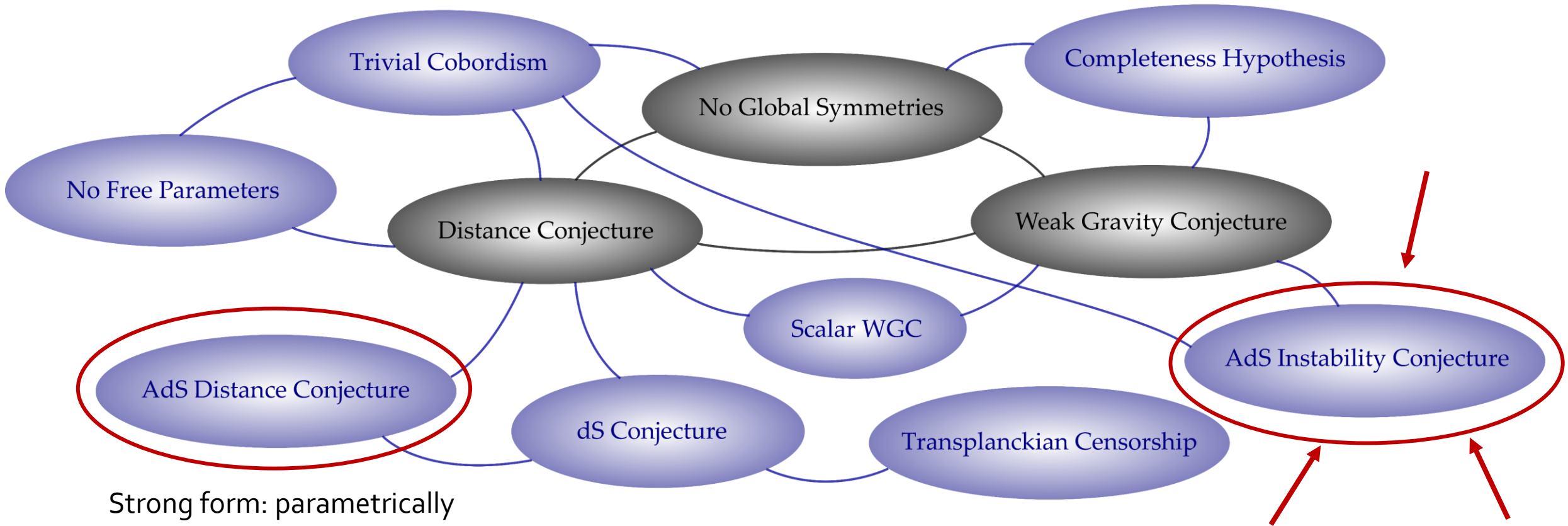
- **Swampland program** in string theory



Adapted from van Beest, Calderón-Infante, Mirfendereski, Valenzuela '21

A swampland in the room

Extracted from van Beest, Calderón-Infante, Mirfendereski, Valenzuela '21



Strong form: parametrically
scale separated SUSY vacua
are in the swampland

AdS instability conjecture

Ooguri, Vafa '16

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AdS instability conjecture

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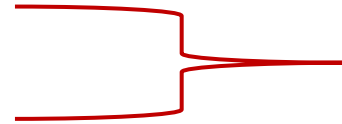
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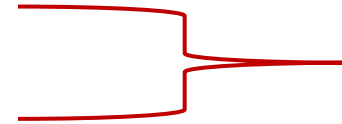
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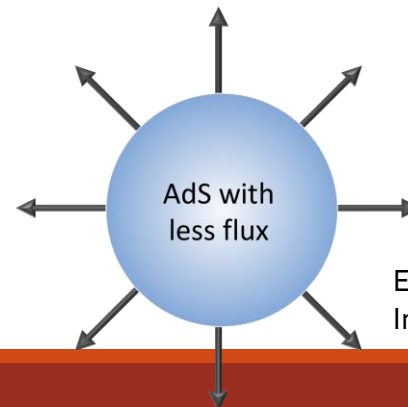
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 - **Consequence II**: this brane corresponds to an instability. Any non-SUSY AdS supported by fluxes is at best metastable.



Maldacena, Michelson, Strominger '99



Extracted from van Beest, Calderón-Infante, Mirfendereski, Valenzuela '21

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- Shown to be satisfied in **many examples**

Apruzzi, Bruno De Luca, Gnechi, Lo Monaco, A. Tomasiello '19; Bena, Pilch, Warner '20; Suh '20; Apruzzi, Bruno De Luca, Lo Monaco, Uhlemann '21; Bomans, Cassani, Dibitetto, Petri '21...

Compactifications of the form **$AdS_4 \times X_6$** , with X_6 admitting a **CY metric**, remain elusive (perturbatively stable)

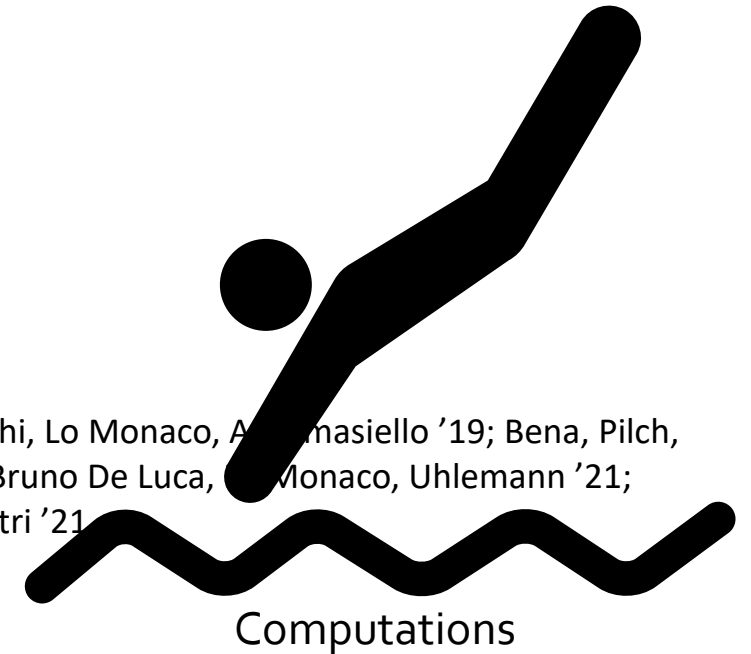
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 - For **Non-SUSY** _{G_4} : **integer** conformal dimensions JQ'22.

$$\begin{aligned} \Delta &= 10, & \Delta_i &= 1 \text{ or } 2, & \Delta_a &= 6, \\ \Delta &= 1 \text{ or } 2, & \Delta_i &= 3, & \Delta_a &= 8 \end{aligned}$$

For $i = 1, \dots, h^{2,1}$ and $a = 1, \dots, h_-^{1,1}$

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 - For **Non-SUSY** _{G_2} : **non-integer** conformal dimensions JQ'22

$$\begin{array}{lll} \Delta = \frac{1}{2}(3 + \sqrt{393}), & \Delta_i = \frac{1}{2}(3 + \sqrt{201}), & \Delta_a = 3, \\ \Delta = \frac{1}{2}(3 + \sqrt{33}), & \Delta_i = 6, & \Delta_a = 3 \end{array} \quad \text{For } i = 1, \dots, h^{2,1} \text{ and } a = 1, \dots, h_-^{1,1}$$

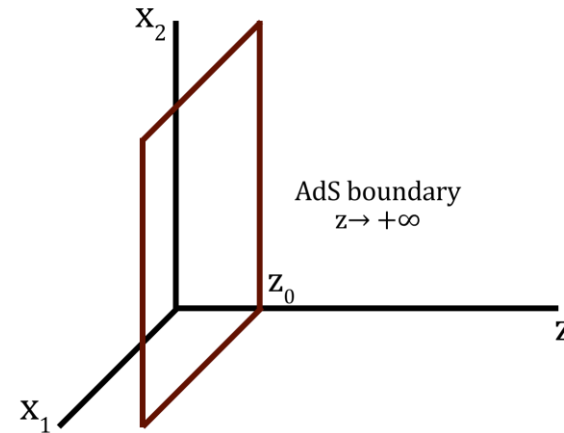
AdS instability conjecture

- According to this conjecture there should be a codimension one object (a DW from the 4d point of view) with $Q > T$
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 - We need to study the membrane spectrum of the theory
- Basic idea: consider the Poincaré for the AdS_4 metric $ds_4^2 = e^{\frac{2z}{R}}(-dt^2 + d\vec{x}^2) + dz^2$. Boundary in $z = +\infty$

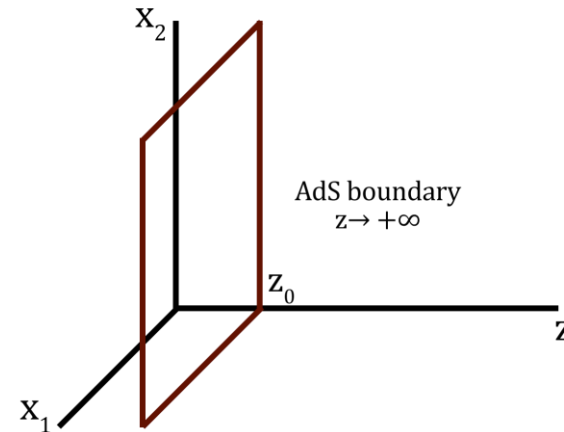
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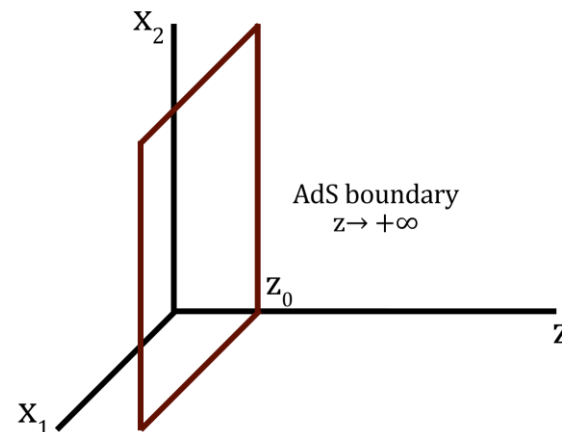


- This can be **avoided** considering the **p -form** potentials to which the membrane couples. Example $C_3 = Qe^{3z_0/R} dt \wedge dx^1 \wedge dx^2$ and $Q = T \rightarrow$ equilibrium. If $Q > T \rightarrow$ instability

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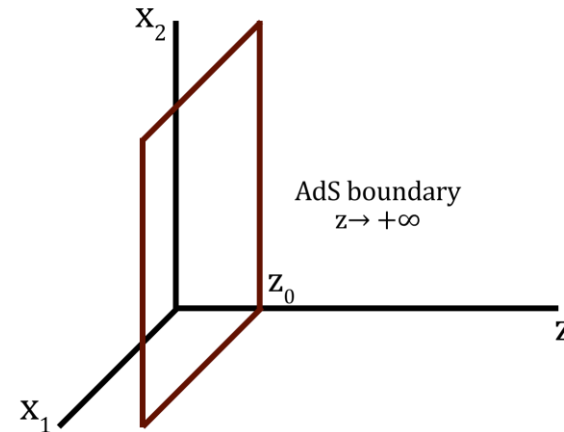


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Due to lack of time we will only focus on the **Non-SUSY** G_4 branch
(remember $G_4 = -G_4^{\text{SUSY}}$)

AdS instability conjecture

- Non-SUSY _{G_4} . The *internal* fluxes:

$$H = \frac{1}{2} F_0 g_s \text{Re} \Omega_{CY}, \quad G_0 = \frac{1}{l_s} m, \quad G_2 = 0, \quad G_4 = -\frac{3G_0}{10} J_{CY}^2, \quad G_6 = 0$$

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$$C_9 = -\frac{5}{3e^\phi} e^{\frac{3z}{R}} dt \wedge dx^1 \wedge dx^2 \wedge d\text{vol}_6 \quad C_5 = -\frac{1}{e^\phi} e^{\frac{3z}{R}} dt \wedge dx^1 \wedge dx^2 \wedge d\text{vol}_{2\text{-cycle}}$$

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- And so the (naïve) **charge** of the **DW branes** will be obtained from the $S_{CS} = \int C \wedge e^{-\mathcal{F}}, \mathcal{F} = B + \frac{l_s}{2\pi} F$:

$$S_{CS}^{D8} = \int C_9 + \frac{1}{2} \int C_5 \wedge \mathcal{F} \wedge \mathcal{F} \quad S_{CS}^{D6} = -\frac{1}{2} \int C_5 \wedge \mathcal{F} \quad S_{CS}^{D4} = -\frac{1}{2} \int C_5$$

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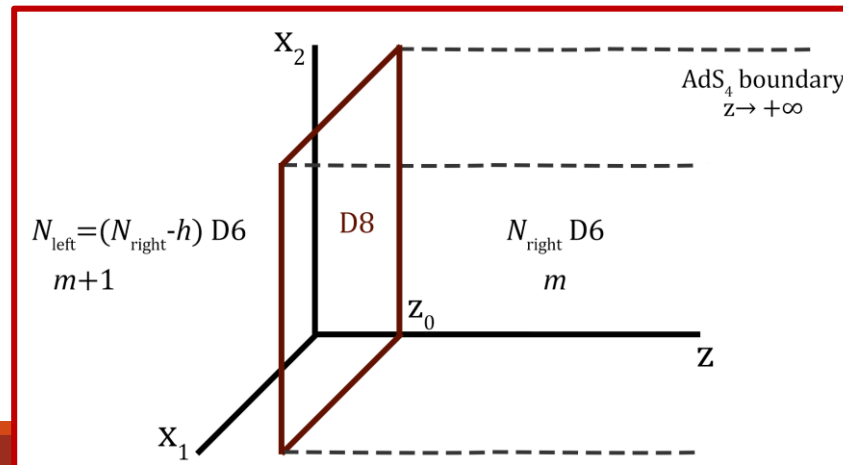
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$$S_{CS}^{D8} = \int C_9 + \frac{1}{2} \int C_5 \wedge \mathcal{F} \wedge \mathcal{F}$$

Freed Witten anomaly for the \mathcal{F} in the D8: $d\mathcal{F} = H + \delta \rightarrow$ need **space-filling** D6 to cancel the tadpole

$$Q_{DW}^{D8} = Q_{CS}^{D8} + Q_{DBI}^{D6}$$



$$Q_{DW}^{D8} = -\frac{1}{2} \int C_5$$


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 - But were working all this time in the smearing approximation... 🙅
 - Using Junghans '20, Marchesano, Palti, JQ, Tomassielo '20, going **beyond** the **smearing** approximation and considering curvature corrections $Q \gtrsim T$
 - First derived in Marchesano, Prieto, JQ '21, Several explicit **toroidal examples** in Casas, Marchesano, Prieto '22.


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 - Already using the smearing approximation $Q > T$
 - Curvature and beyond smearing corrections suppressed compared to the leading term
 - Though focused on the Non-SUSY_{G₄} branch, the same seems to apply for the Non-SUSY_{G₂} branch
- AdS instability conjecture strongly satisfied → non-perturbative instability
- More work still to be done. Please stay tuned!



Conclusions

- Studied some properties (CFT dual, stability) of two non-SUSY DGKT vacua: Non-SUSY _{G_4} ($G_4 = -G_4^{\text{SUSY}}$) and Non-SUSY _{G_2} ($G_2^{\text{harmonic}} \neq 0$)
- Would-be CFT dual: for the Non-SUSY _{G_4} integer conformal dimensions, for the Non-SUSY _{G_2} non-integer conformal dimensions
- AdS instability conjecture: seems to be satisfied easily in both set-ups through DW D8 branes with internal $\mathcal{F} \sim J$. D6s ending on them to cancel the tadpoles. Need more work
- The problem of getting scale separated and (sufficiently meta)stable non-SUSY vacua still open

Conclusions

- Studied some properties (CFT dual, stability) of two non-SUSY DGKT vacua: Non-SUSY _{G_4} ($G_4 = -G_4^{\text{SUSY}}$) and Non-SUSY _{G_2} ($G_2^{\text{harmonic}} \neq 0$)
- Would-be CFT dual: for the Non-SUSY _{G_4} integer conformal dimensions, for the Non-SUSY _{G_2} non-integer conformal dimensions
- AdS instability conjecture: seems to be satisfied easily in both set-ups through DW D8 branes with internal $\mathcal{F} \sim J$. D6s ending on them to cancel the tadpoles. Need more work
- The problem of getting scale separated and (sufficiently meta)stable non-SUSY vacua still open

Thank you for your attention! 😊